



# Cambridge IGCSE™

CANDIDATE NAME



CENTRE NUMBER

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**CAMBRIDGE INTERNATIONAL MATHEMATICS**

**0607/41**

Paper 4 (Extended)

**October/November 2024**

**2 hours 15 minutes**

You must answer on the question paper.

You will need: Geometrical instruments

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly and you will be given marks for correct methods, including sketches, even if your answer is incorrect.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For  $\pi$ , use your calculator value.

## INFORMATION

- The total mark for this paper is 120.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages.



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1  
7  
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4  
1  
3  
6  
5  
9  
7  
x



## Formula List

For the equation  $ax^2 + bx + c = 0$   $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Curved surface area,  $A$ , of cylinder of radius  $r$ , height  $h$ .  $A = 2\pi rh$

Curved surface area,  $A$ , of cone of radius  $r$ , sloping edge  $l$ .  $A = \pi rl$

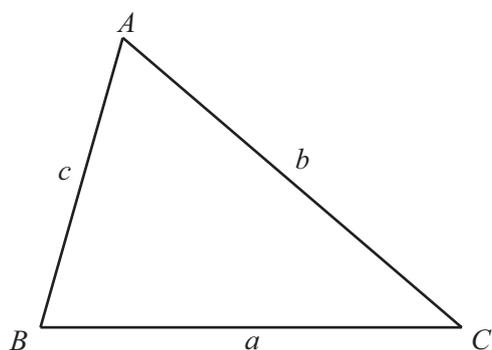
Curved surface area,  $A$ , of sphere of radius  $r$ .  $A = 4\pi r^2$

Volume,  $V$ , of pyramid, base area  $A$ , height  $h$ .  $V = \frac{1}{3}Ah$

Volume,  $V$ , of cylinder of radius  $r$ , height  $h$ .  $V = \pi r^2 h$

Volume,  $V$ , of cone of radius  $r$ , height  $h$ .  $V = \frac{1}{3}\pi r^2 h$

Volume,  $V$ , of sphere of radius  $r$ .  $V = \frac{4}{3}\pi r^3$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{Area} = \frac{1}{2}bc \sin A$$





Answer **all** the questions.

1 (a) Solve the equations.

(i)  $6x + 5 = -19$

$x = \dots\dots\dots$  [2]

(ii)  $8x - 13 = 11 - 4x$

$x = \dots\dots\dots$  [2]

(iii)  $\frac{8}{2x-3} = -5$

$x = \dots\dots\dots$  [3]

(b) Solve the equation  $6x^2 - 2x - 1 = 0$ .

Give your answers correct to 2 decimal places.  
You must show all your working.

$x = \dots\dots\dots$  or  $x = \dots\dots\dots$  [3]



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2 (a) Younous wants to calculate  $\frac{78.8}{2.46^2} + \frac{153 + 9.81^2}{\sqrt{9.47}}$ .

(i) He finds an estimate for the answer by rounding each number correct to 1 significant figure.

Find this estimate.

You must show all your working.

..... [2]

(ii) Explain why his answer to **part (i)** is greater than the actual answer.

..... [1]  
 .....

(iii) Work out.

$$\frac{78.8}{2.46^2} + \frac{153 + 9.81^2}{\sqrt{9.47}}$$

..... [1]





(b) Work out  $3\frac{1}{4} \times \frac{8}{39}$ .

..... [1]

(c) (i) Write 506 grams in kilograms.

..... kg [1]

(ii) Write 2000 m<sup>2</sup> in km<sup>2</sup>.

..... km<sup>2</sup> [1]

(d) An athlete runs 20 km in 100 minutes and then walks at 8 km/h for 50 minutes.

Find the athlete's average speed in km/h.

..... km/h [3]

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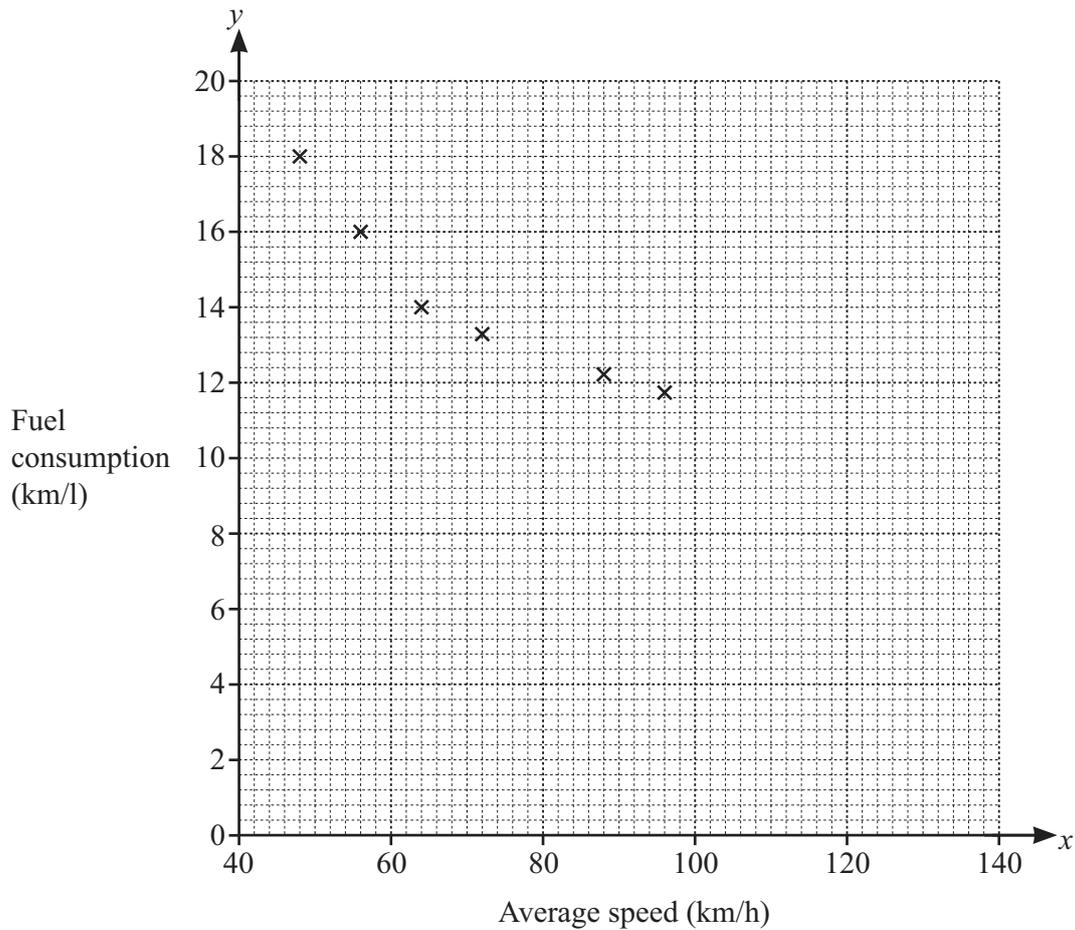


3 Paulo compares the fuel consumption of his car and the average speed of his car for ten journeys.

The results are shown in the table.

Average speed ( $x$ kilometres per hour)	48	56	64	72	88	96	104	120	128	136
Fuel consumption ( $y$ kilometres per litre)	18	16	14	13.3	12.2	11.8	11.4	9.2	8	7

- (a) (i) Complete the scatter diagram.  
The first six points have been plotted for you.



[2]

- (ii) What type of correlation is shown by the scatter diagram?

..... [1]





(b) Find the mean fuel consumption.

..... km/l [1]

(c) (i) Find the equation of the regression line for  $y$  in terms of  $x$ .

$y =$  ..... [2]

(ii) Use your regression line to estimate the fuel consumption when the average speed is 80 km/h.

..... km/l [1]

(iii) Paulo drives his next journey at an average speed of 30 km/h.

Give a reason why the regression line is unlikely to give a reliable estimate of the fuel consumption for this journey.

..... [1]

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4 (a) Alan, Beth and Imran share an amount of money in the ratio  $3x : 2x : (x + 1)$  where  $x$  is an integer.

(i) Find the amount Beth receives when  $x = 4$  and they share \$400 in total.

\$ ..... [3]

(ii) Find the amount that Alan receives when Beth receives \$66.

\$ ..... [2]

(iii) Find the value of  $x$  when Alan receives 2.5 times the amount Imran receives.

$x =$  ..... [2]

(b) In a sale, a shop reduces the price of all furniture by 12%.

(i) Find the sale price of a chair that has an original price of \$90.

\$ ..... [2]

(ii) Find the original price of a table that has a sale price of \$440.

\$ ..... [2]

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- (c) Kurt invests  $\$X$  in a bank which pays simple interest at a rate of 4% each year. The total amount of money that Kurt has in the bank at the end of 6 years is  $\$930$ .

Show that  $X = 750$ .

[2]

- (d) Ivana invests  $\$750$  in a bank which pays compound interest at a rate of  $y\%$  each year. The total amount of money that Ivana has in the bank at the end of 6 years is  $\$921.94$ .

Find the value of  $y$ .

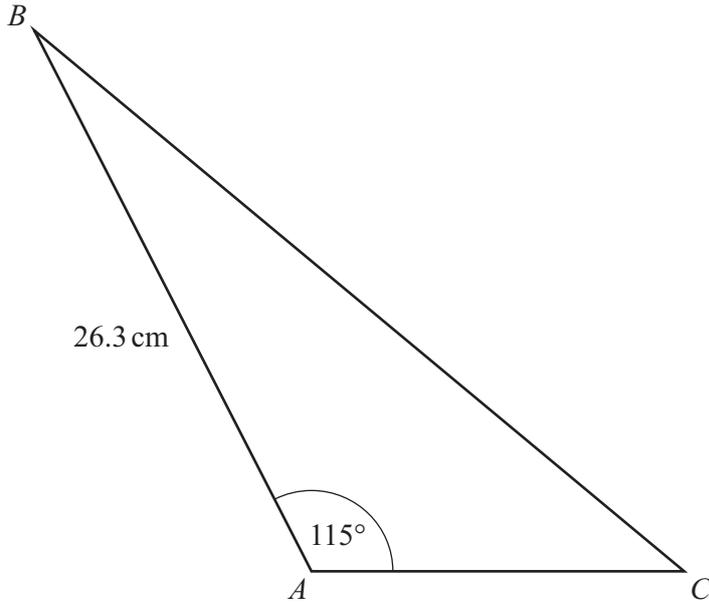
$y = \dots\dots\dots$  [3]

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5



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The area of triangle  $ABC$  is  $262 \text{ cm}^2$ .

(a) Show that  $AC = 22.0 \text{ cm}$ , correct to 1 decimal place.

[2]

(b) Find  $BC$ .

$BC = \dots\dots\dots \text{ cm}$  [3]



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(c) Use the sine rule to find angle  $ABC$ .

Angle  $ABC = \dots\dots\dots [3]$

(d) Find the length of the perpendicular line from  $A$  to the line  $BC$ .

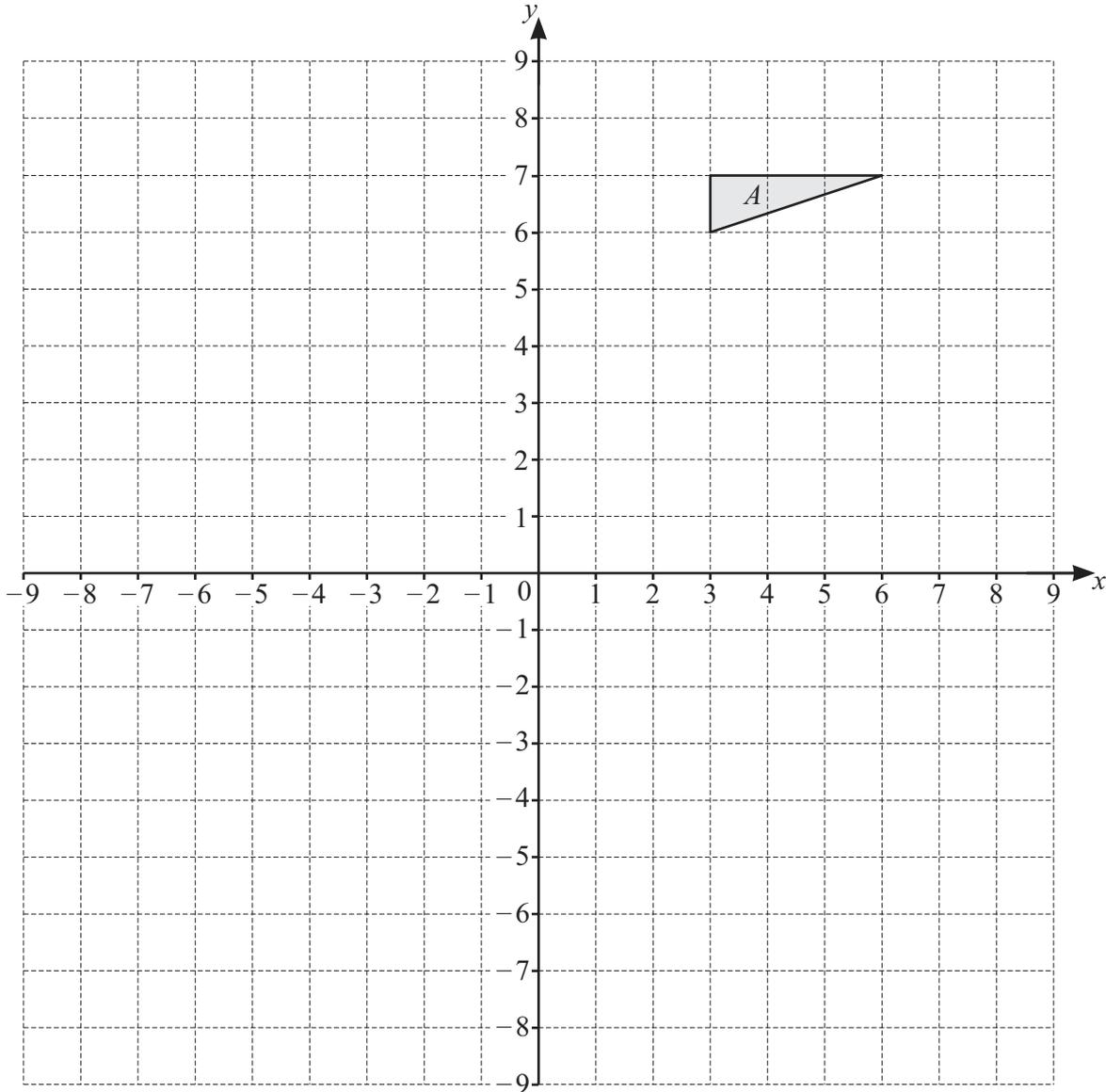
$\dots\dots\dots$  cm [2]

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6 (a)



- (i) Draw the image of triangle *A* after a reflection in the line  $y = -x$ .  
Label the image *B*. [2]
- (ii) Draw the image of **triangle B** after a reflection in the *y*-axis.  
Label the image *C*. [1]
- (iii) Describe fully the **single** transformation that maps **triangle C** onto **triangle A**. [3]

.....

.....





(b) The transformation P is a translation with vector  $\begin{pmatrix} -1 \\ 3 \end{pmatrix}$ .

The transformation Q is a stretch, factor 3 with invariant line  $y = 2$ .

(i) Describe the transformation that is the inverse of P.

..... [2]

(ii) Describe the transformation that is the inverse of Q.

..... [2]

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7 (a) There are 49 students in a year group.

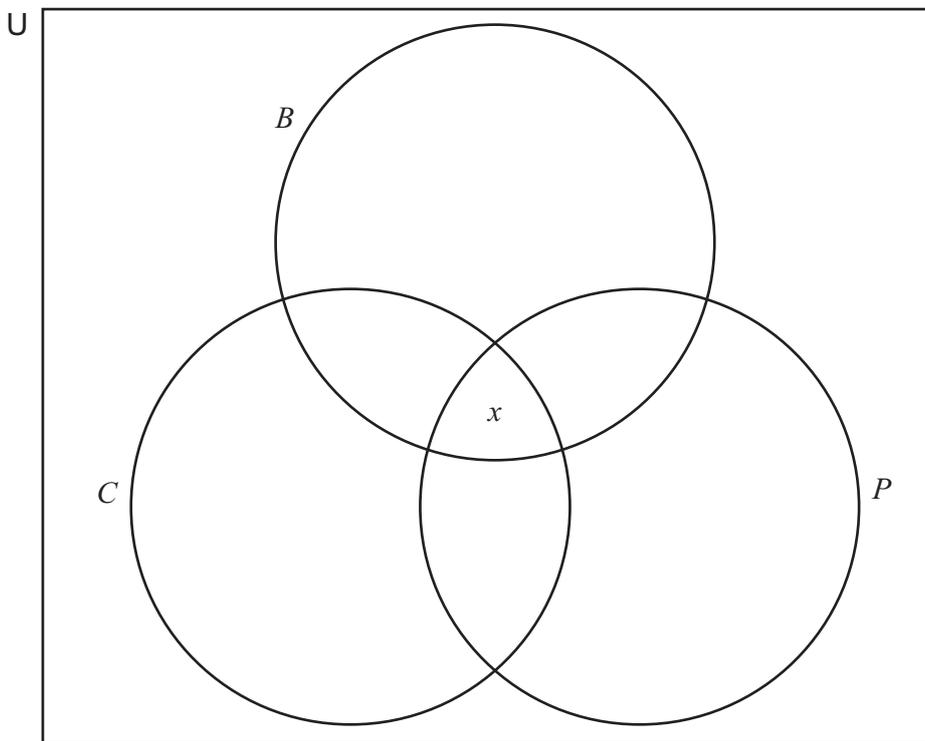
Each student studies at least one of the sciences, biology (*B*), chemistry (*C*) and physics (*P*).

$x$  students study all 3 sciences.  
 $y$  students study chemistry only.  
12 students study physics only.

6 students study biology and chemistry but not physics.  
11 students study biology and physics but not chemistry.  
2 students study physics and chemistry but not biology.

25 students study only one science.

(i) Show this information on the Venn diagram.



[2]

(ii) Find the number of students who study all 3 sciences.

..... [2]

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(iii) The number of students that study biology is two times the number of students that study chemistry.

Find the number of students who study

(a) chemistry only

..... [2]

(b) biology only.

..... [1]

(b) A bag contains 7 red balls and 3 blue balls.  
In an experiment, three balls are chosen at random without replacement.

Find the probability that at least two of the balls chosen are red.

..... [4]

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8 Find the next term and the  $n$ th term in each of the following sequences.

(a) 16, 9, 2, -5, -12, ...

next term = .....

$n$ th term = ..... [3]

(b) 2, 8, 18, 32, 50, ...

next term = .....

$n$ th term = ..... [3]

(c) 1, -3, 5, -7, 9, ...

next term = .....

$n$ th term = ..... [3]

(d) 6, 9, 10, 9, 6, ...

next term = .....

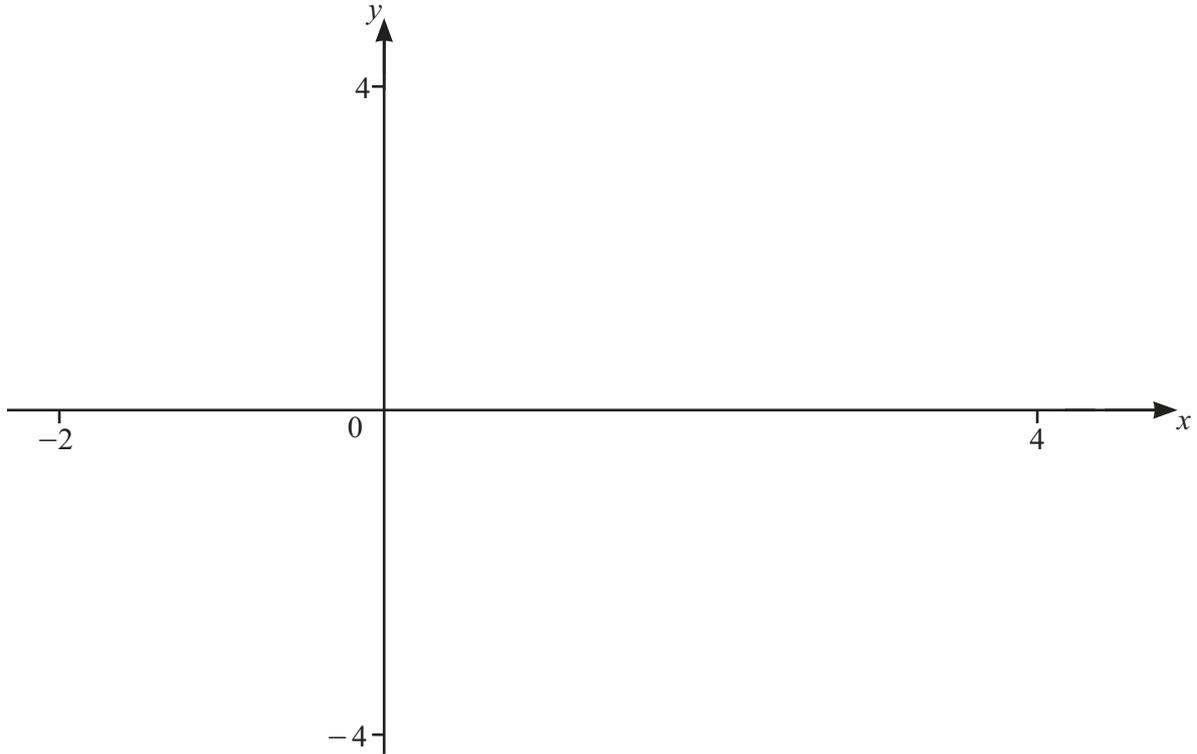
$n$ th term = ..... [3]

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9



$$f(x) = \frac{1}{(2x - 3)(2x + 1)}$$

(a) On the diagram, sketch the graph of  $y = f(x)$  for values of  $x$  between  $-2$  and  $4$ . [3]

(b) Write down the equations of the asymptotes parallel to the  $y$ -axis.  
 ..... [2]

(c) Write down the coordinates of the local maximum.  
 ( ..... , ..... ) [2]

(d) The line  $y = x - 2$  intersects the curve  $y = f(x)$  three times.  
 Find the  $x$ -coordinate of each point of intersection.  
 $x = \dots\dots\dots$  or  $x = \dots\dots\dots$  or  $x = \dots\dots\dots$  [3]

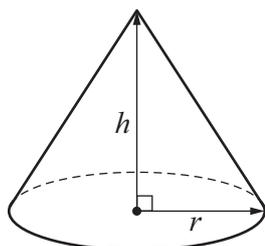
(e) Solve the inequality  $f(x) \geq x - 2$ .  
 ..... [3]

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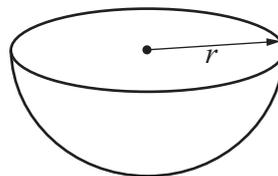




10 In this question all lengths are in centimetres.



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A solid cone has radius  $r$  and vertical height  $h$ .

A solid hemisphere also has radius  $r$ .

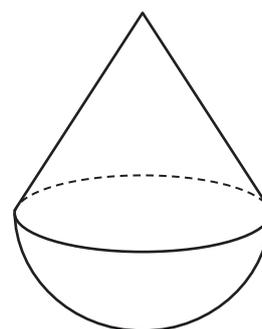
The curved surface area of the cone is the same as the curved surface area of the hemisphere.

(a) Show that  $h = r\sqrt{3}$ .

[4]

(b) The cone is placed directly on top of the hemisphere.

Show that the volume of this solid is  $\frac{1}{3}\pi r^3(2 + \sqrt{3})$ .



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[2]





(c) A larger solid is mathematically similar to the solid in **part (b)**.

The larger solid has volume  $243\pi r^3(2 + \sqrt{3})$ .

(i) Find, in terms of  $r$ , the radius of the hemisphere of the larger solid.

..... [2]

(ii) The surface area of the larger solid is  $5000 \text{ cm}^2$ .

Find the volume of this solid.

.....  $\text{cm}^3$  [4]

**Question 11 is printed on the next page.**



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11 (a) Solve the equation.

$$2 \log 5 - 5 \log 2 = 3 \log 4 - 2 \log x$$

Give your answer in the form  $\frac{a\sqrt{b}}{c}$ , where  $a$ ,  $b$  and  $c$  are integers.

$x = \dots\dots\dots$  [4]

(b) Make  $x$  the subject of the formula.

$$y = \sqrt{\frac{x}{2x+1}}$$

$x = \dots\dots\dots$  [4]

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